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Examples 6.1 – The Cosine and Sine Functions

1. Suppose $y = -4\sin(3x + \frac{7\pi}{5}) = -4\sin(3(x + \frac{7\pi}{15}))$. Determine the amplitude, period, and phase shift of the graph.

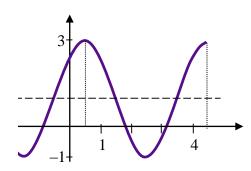
Solution:

2. Let us call the horizontal line about which the graph oscillates the **midline**. With no vertical shift, the midline of a general cosine or sine function is the line y = 0. Determine the amplitude, period, phase shift, and midline of the sinusoidal function $y = 5\cos(3\pi x) - 2$.

Solution:

3. For the graph shown on the right, find a sinusoidal formula of the form $y = A\cos(Bx - C) + D$.

Solution:



4. We know that $y = \sin x$ is zero for $x = n\pi$ (n an integer), and $y = \cos x$ is zero for $x = \frac{m\pi}{2}$ (m an odd integer). What are the roots (x-intercepts) of $y = \sin\left(\frac{3\pi}{2}x - 1\right)$ and $y = \cos\left(5x + \frac{\pi}{2}\right)$?

Solution: