Examples 8.3 – Rolle's Theorem and the Mean Value Theorem

1. Show that $f(x) = \frac{1}{2}x - \sqrt{x}$ satisfies the hypothesis of Rolle's Theorem on [0, 4], and find all values of c in (0, 4) that satisfy the conclusion of the theorem.

Solution:

2. Show that $f(x) = \sqrt{25 - x^2}$ satisfies the hypothesis of the Mean Value Theorem on [-5, 3], and find all values of c in (-5, 3) that satisfy the conclusion of the theorem.

Solution: