## Examples 7.5 - Differential Equations

1. A cup of coffee at $200^{\circ} \mathrm{F}$ is allowed to cool in a room with a constant temperature of $75^{\circ} \mathrm{F}$. If the temperature of the coffee is $185^{\circ} \mathrm{F}$ after 3 min , what will the temperature be after 10 min ?

## Solution:

2. Find the general solution to the differential equation $y^{\prime \prime}=9 y$, and then find the constants $C_{1}$ and $C_{2}$ in the general solution given that $y(0)=1$ and $y^{\prime}(0)=15$.

## Solution:

3. A mass attached to a vertical spring has position $y(t)$ meters after $t$ seconds, where $y$ satisfies $y^{\prime \prime}=-4 y$. Positions below equilibrium and downward motion are considered positive.
(a) Find the position function if the initial position is 0.5 m and the initial velocity is $3 \mathrm{~m} / \mathrm{s}$.

## Solution:

(b) Find a time at which the mass is at its greatest distance from equilibrium. Use this answer to find the amplitude of the system.

## Solution:

