Examples 7.5 – Differential Equations

1. A cup of coffee at 200°F is allowed to cool in a room with a constant temperature of 75°F. If the temperature of the coffee is 185°F after 3 min, what will the temperature be after 10 min?

Solution:

2. Find the general solution to the differential equation y'' = 9y, and then find the constants C_1 and C_2 in the general solution given that y(0) = 1 and y'(0) = 15.

Solution:

- 3. A mass attached to a vertical spring has position y(t) meters after t seconds, where y satisfies y'' = -4y. Positions below equilibrium and downward motion are considered positive.
 - (a) Find the position function if the initial position is 0.5 m and the initial velocity is 3 m/s.Solution:

(b) Find a time at which the mass is at its greatest distance from equilibrium. Use this answer to find the amplitude of the system.

Solution: