Examples 7.3 – Graph Analysis with the TI-84

We demonstrate each of the first six choices in the "calculate" menu and postpone definite integration until Chapter 8.

Consider the functions $f(x) = (x-2)^3 - 5x + 12$ and g(x) = 3x - 2 for x in the interval [0, 5]. In the function menu, we enter $Y_1 = (X-2)^{3} - 5X + 12$ and $Y_2 = 3X - 2$, and we set the viewing window as $[0, 5] \times [-6, 7]$.

- 1: Suppose we want f(1) and g(1). Choose 1:value, input x = 1, and press [ENTER]. Toggle between Y_1 and Y_2 with the up and down arrow keys.
- 2: Note that f has an x-intercept between x = 2 and x = 3. To find it, choose 2:zero, and toggle to Y₁. Using the arrow keys, position the cursor slightly to the left of the intercept and press [ENTER]. Then position the cursor slightly to the right of the intercept and press [ENTER]. Finally, position the cursor between the chosen bounds, near the intercept, and press [ENTER].
- 3: A local minimum of f occurs between x = 3 and x = 4. Choose 3:minimum, and toggle to Y₁. Using the arrow keys, position the cursor slightly to the left of the minimum and press **[ENTER]**. Then position the cursor slightly to the right of the minimum and press **[ENTER]**. Finally, position the cursor between the chosen bounds, near the minimum, and press **[ENTER]**.
- 4: Choose 4:maximum and repeat the same steps to find the local maximum of f between x = 0 and x = 1.
- 5: The graphs of f and g intersect once in the given window. Choose 5:intersect, press [ENTER] when asked if Y₁ is the "first curve," and press [ENTER] when asked if Y₂ is the "second curve." Position the cursor near the intersection point and press [ENTER].
- 6: To find f'(2.8), for instance, choose 6:dy/dx, toggle to Y_1 , input x = 2.8, and press **[ENTER]**.

Finding an inflection point: Although the TI-84 has no menu option for finding the inflection point of f, we can get around this by finding the extrema of $f'(x) = 3(x-2)^2 - 5$. Enter $Y_3=3(X-2)^2-5$, and note that f' has a minimum. This point represents the point on the graph of f of maximum decrease. Use 3:minimum to find the *x*-coordinate of the inflection point. Plug this *x* back into f to find the *y*-coordinate of the inflection point.