



### Examples 7.3 – Graph Analysis with the TI-84

We demonstrate each of the first six choices in the “calculate” menu and postpone definite integration until Chapter 8. Follow along with your own calculator.

Consider the functions  $f(x) = (x-2)^3 - 5x + 12$  and  $g(x) = 3x - 2$  for  $x$  in the interval  $[0, 5]$ . In the function menu, we enter  $\backslash Y_1 = (X-2)^3 - 5X + 12$  and  $\backslash Y_2 = 3X - 2$ , and we set the viewing window as  $[0, 5] \times [-6, 7]$ .

- 1: Suppose we want  $f(1)$  and  $g(1)$ . Choose `1:value`, input  $x = 1$ , and press **[ENTER]**.  
Toggle between  $Y_1$  and  $Y_2$  with the up and down arrow keys.
- 2: Note that  $f$  has an  $x$ -intercept between  $x = 2$  and  $x = 3$ . To find it, choose `2:zero`, and toggle to  $Y_1$ . Using the arrow keys, position the cursor slightly to the left of the intercept and press **[ENTER]**. Then position the cursor slightly to the right of the intercept and press **[ENTER]**. Finally, position the cursor between the chosen bounds, near the intercept, and press **[ENTER]**.
- 3: A local minimum of  $f$  occurs between  $x = 3$  and  $x = 4$ . Choose `3:minimum`, and toggle to  $Y_1$ . Using the arrow keys, position the cursor slightly to the left of the minimum and press **[ENTER]**. Then position the cursor slightly to the right of the minimum and press **[ENTER]**. Finally, position the cursor between the chosen bounds, near the minimum, and press **[ENTER]**.
- 4: Choose `4:maximum` and repeat the same steps to find the local maximum of  $f$  between  $x = 0$  and  $x = 1$ .
- 5: The graphs of  $f$  and  $g$  intersect once in the given window. Choose `5:intersect`, press **[ENTER]** when asked if  $Y_1$  is the “first curve,” and press **[ENTER]** when asked if  $Y_2$  is the “second curve.” Position the cursor near the intersection point and press **[ENTER]**.
- 6: To find  $f'(2.8)$ , for instance, choose `6:dy/dx`, toggle to  $Y_1$ , input  $x = 2.8$ , and press **[ENTER]**.

**Finding an inflection point:** Although the TI-84 has no menu option for finding the inflection point of  $f$ , we can get around this by finding the extrema of  $f'(x) = 3(x-2)^2 - 5$ . Enter  $\backslash Y_3 = 3(X-2)^2 - 5$ , and note that  $f'$  has a minimum. This point represents the point on the graph of  $f$  of maximum decrease. Use `3:minimum` to find the  $x$ -coordinate of the inflection point. Plug this  $x$  back into  $f$  to find the  $y$ -coordinate of the inflection point.