



## Activity 5.6 – Definite Integrals of Exponentials and Logarithms

1. (a)  $\Delta x = 0.4$

(b)  $\int_0^2 3e^{x^2} dx \approx \left( 3e^{(0.2)^2} + 3e^{(0.6)^2} + 3e^{(1)^2} + 3e^{(1.4)^2} + 3e^{(1.8)^2} \right) \cdot 0.4 \approx 45.390565$

2. (a)  $\int_{-1}^1 e^{5.2x} dx = \left( \frac{e^{5.2x}}{5.2} \right) \Big|_{-1}^1 = \frac{e^{5.2}}{5.2} - \frac{e^{-5.2}}{5.2} \approx 34.86$

(b)  $\int_0^1 10^x dx = \left( \frac{10^x}{\ln 10} \right) \Big|_0^1 = \frac{10}{\ln 10} - \frac{1}{\ln 10} \approx 3.91$

3. (a) The initial rate is  $a = 0.5$ , so  $R(t) = 0.5b^t$ . Also,  $R(120) = 0.5b^{120} = 0.25$ . From this last equation,  $b^{120} = 0.5$ , so  $b = \sqrt[120]{0.5} \approx 0.9942$ . The formula for  $R(t)$  is  $R(t) = 0.5(0.9942)^t$  million gallons per minute.

(b)  $R(280) = 0.5(0.9942)^{280} \approx 0.0981$  million gallons per minute.

(c)  $\int_0^{280} 0.5(0.9942)^t dt = \left( \frac{0.5(0.9942)^t}{\ln(0.9942)} \right) \Big|_0^{280} \approx 69.0938$  million gallons

4. (a)  $\int_1^x \frac{1}{t} dt = (\ln |t|) \Big|_1^x = \ln |x| - \ln |1| = \ln x$

(b)  $\int_1^x \frac{1}{t} dt = \ln x = 1$  implies that  $x = e$ .